

# An Alternative Hypothesis for Special Relativity

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An alternative theory being analogous to Einstein's special theory of relativity is presented. While Einstein based his theory on the relativity principle of motion and constancy of the velocity of light, this theory assumes an absolute frame of reference and a general length contraction. Both concepts are taken from general relativity and applied to an asymptotically flat space. This results in a transformation group being different from the Lorentz transformation and a Euclidian addition theorem of velocities. The results are in accordance with experiments and long known discrepancies between special relativity and experimental findings are resolved as well as paradoxa being introduced by Einstein's original theory. Physical facts being unintelligible before can be interpreted in the light of the alternative theory.

## 1 Introduction

The theory of special relativity of Albert Einstein is essentially based on the constancy of the velocity of light in all inertial frames of reference. Einstein introduced this as a physical principle or axiom in order to explain the negative outcome of the experiments of Michelson and Morley who tried to prove the existence of a drift velocity of the earth in a hypothetical ether. However, in the last years a number of experiments came up showing that the velocity of light is not an incontrovertible constant. For example Nimtz [5, 6] has realised a transfer of information by microwaves by speeds faster than light. His explanations are wound and based on quantum effects (tunnelling) which should not appear in systems with exclusively macroscopic dimensions. Most convincing would be an explanation by classical physics which is also the basis of electromagnetic signal transmission. Another important development is the re-interpretation of the Michelson-Morley experiments [10, 11] which show that they had not been evaluated in the right way. When doing this, earlier inconsistencies are resolved and an absolute motion of the earth against the space background is detected. This revolutionary insight has not been recognized in the scientific public so far. Therefore re-thinking about the concepts of special relativity is required.

A second fundament of modern physics is the principle of relativity. Besides the reasonable assumption that laws of nature work in the same way in all reference frames not being accelerated to one another, it is postulated that the transformation between reference frames is always of the same form. It is assumed that all frames of reference be of equal kind. This consideration does not take into account that the universe is structured by masses which define reference points for physical processes. The whole universe is impleted with gravitational and electromagnetic fields. This also holds for the "empty" ranges between galaxies and galaxy clusters since the particle density is non-vanishing in interstellar space to

today's knowledge. So we can say that in certain areas of the cosmos we can neglect the influence of cosmic fields, but normally we use the visible beacons (earth, sun, centers of galaxies) to define reference frames. The cosmos as a whole is described by general relativity and Mach's principle which states that the masses define the space. Without masses there is no space at all. Crothers [4] has pointed out that there is no smooth transition from general to special relativity:

"Special Relativity is merely an augmentation to Minkowski space by the arbitrary insertion of mass and energy into Minkowski space with the constrained kinematic features of Minkowski space applied to those masses and energies".

This view is corroborated by newer advanced theories like Einstein-Cartan-Evans theory [18] where space is not empty but filled with the background or "vacuum" potential. Without potential there is no space, in accordance with Mach's principle. So it should become clear that general relativity (or any similar advanced theory) is necessarily required to define a basis for all physics. One can abstract then from these foundations and concentrate on other problems, for example experiments of particle collisions, without taking care of these basic premises. When it comes to define the frames of reference, however, the state of motion relative to the absolutely defined environment is important again.

All these arguments become much more intelligible if we assume that the space between massive particles has a state of motion. This sounds like introducing the old ether idea from the nineteenth century. Our knowledge has only little improved since then. The ether was abolished by Einstein, but indirectly re-introduced by himself in his theory of general relativity. It is possible to define an "objective" frame of reference constituted by existing masses. Considering Einstein-Cartan-Evans theory, space is not empty but itself a medium which for example has optical properties [18]. We can extend the comparison with usual media by assigning a state of

motion to the space itself. Masses “swim” in this space and therefore reflect its movement. Conversely, the fields created by the masses determine the surrounding space in a fed-back manner. Both entities cannot be considered independently from each other.

In Einstein-Cartan-Evans theory, the covariance principle is the most general description base of physics, indicating that all laws of nature are independent of the coordinate system or reference frame. Our physical environment is defined by the objectively existing structure which is defined by masses, charges and fields. These are adequately described in an objective manner by laws of nature being independent from subjective human receptions.

In this article we try to modify Einstein’s axioms of special relativity in such a way that constancy of light velocity is not required to be introduced axiomatically. It will be shown that this is an artifact of measurement. Instead of this axiom we demand for an absolute frame of reference. As a consequence, we will arrive at transformation laws similar to Einstein’s which depend on the absolute reference frame but change asymptotically to Einstein form in certain important application cases. In particular we will obtain a different addition theorem of velocities allowing for superluminal speed. The well known Lorentz transformation and symmetry will evolve not to be valid in our new framework. A more general four-dimensional affine transformation will take its place which has mathematical group properties as well. We will end with a short discussion of the experiments mentioned in this introduction in the light of the new theory.

## 2 Problems in experimental proofs of Special Relativity

In the well-known experiment of Michelson and Morley, which was repeated several times at the beginning of the twentieth century (see a review in [11]), it was apparently shown that the velocity of light  $c$  is the same in all directions relative to the earth orbit. This was considered to be a proof that this velocity is a general constant in nature under all circumstances. We will critically analyse this in the following.

Firstly we have to comment that this is valid only in special relativity, i.e. for unaccelerated motion. In general relativity  $c$  depends on the gravitational field (or on all fields in case of unified field theories). This dependence is well proven experimentally. Therefore we should state that constancy of  $c$  is only valid in vacuo with neglectation of all fields.

Secondly we inspect the way in which measurements of the speed of light were done. These were carried out by interferometers where the runtime of light rays was compared between rays having been reflected in different directions. If there is a directional dependence on propagation speed, a characteristic interferometric pattern should occur if the apparatus is rotated. Within assumed experimental uncertainties, no such pattern was observed. Since the length of the apparatus was not changed it was concluded that the velocity

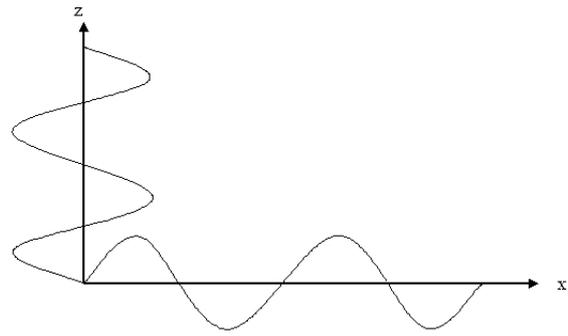


Fig. 1: Length contraction in experiments of Michelson Morley type.

of light was the same in all directions. What not has been considered in this explanation is the effect of length contraction. According to Einstein’s special relativity, the measured length changes with the same factor as the measured time, if the frame of reference is changed by modifying relative speed between observer and object. For the experiments of Michelson-Morley type this means that the run-time of light as well as the interferometer length change, as soon as the apparatus is rotated relative to a hypothetical absolute direction of motion (“ether wind”). The compression factor is the same for length and time, therefore we obtain for two directions with length  $l$  and  $l'$  and run-time  $t$  and  $t'$ :

$$c = \frac{l}{t} = \frac{l'}{t'} = \text{const.} \quad (1)$$

According to Fig. 1 the number of wave trains is the same irrespective of the compression factor. No wonder the value of  $c$  is constant. This type of experiments does not prove the details of the Lorentz transformation.

The re-evaluation of experiments of Michelson-Morley type by Cahill et al. [10, 11] has revealed that the evaluation of experimental data was done by erroneously assuming no length contraction. As explained above, taking length contraction into account leads to a meaningless null experiment. This is the outcome of modern laser interferometer spectroscopy in vacuo. However, the older experiments were performed by interferometers in air or helium. Therefore the refraction index is different from unity (although nearby). Doing the evaluation with respectation of length contraction as well as refractive index effects leads indeed to a non-null result. Surprisingly, all the older experiments, evaluated in this way, then prove a velocity of the earth orbit relative to the space background of 365 km/s within error bars, see Fig. 2 taken from [10, 11]. This is the most significant experimental hint for the physical relevance of a background field. However, it must be added that the most precise value in Fig. 2, measured from the constant background radiation by the COBE satellite, is controversial. Robitaille [17] has argued that the background radiation is an earth-made effect due to the black body radiation of the oceans. Further satellite missions will clear this up.

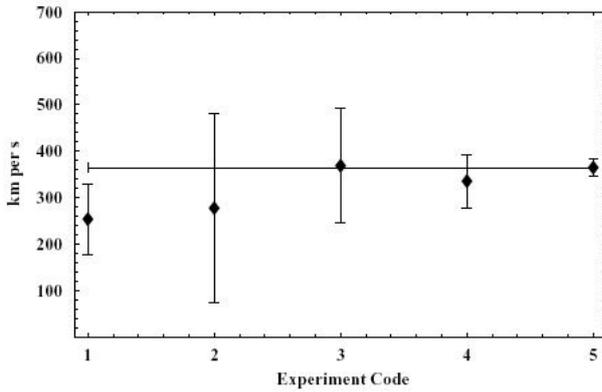


Fig. 2: Speed of earth orbit (reproduction from [10]) in km/s, determined from various Michelson interferometer experiments (1)–(4) and COBE (5): (1) Michelson-Morley (noon observations), (2) Michelson-Morley (18h observations), (3) Illingworth, (4) Miller, Mt. Wilson, and finally in (5) the speed from the COBE satellite observation of the CBR (Constant Background Radiation) microwave spectrum dipole term.

A third problem concerns the interpretation of length contraction and time dilation. Originally Einstein believed that these changes are virtual, i.e. are only measured values of an observer moving relative to another system. The scales of the real objects never change. Later after upcoming of general relativity it became clear that scales have to change in reality because the gravitational field is real in the sense that it evokes real, measurable forces. So it was implicitly assumed that also the scale changes of special relativity have to be real. This however is a severe philosophical problem since two observers measuring the same object would obtain different values for identical physical properties of the object. This discrepancy has not been addressed in literature until today and reflects inconsistencies in the transition from general to special relativity.

### 3 Length contraction

Since length contraction is the central property of this theory as well as Einstein’s special relativity, we will give an explanation how this can be interpreted as a geometric property of fast moving circular or spherical objects. We assume a simple model of matter where atoms are built from an atomic nucleus and orbiting electrons moving in spherical orbits. An observer may travel relative to such an atom with velocity  $v$ , and the orbital tangential velocity of an electron may be  $v_e$  (near to speed of light). Then the observer sees the electron moving on a curve which is a cycloid or trochoid, see Fig. 3. The form of the curve depends on the ratio of radii  $a/b$ , where  $a$  is the radius of the “rolling” circle and  $b$  is the radius of the path of the electron. For the uniform velocity  $v$  we have

$$v = \omega a \tag{2}$$

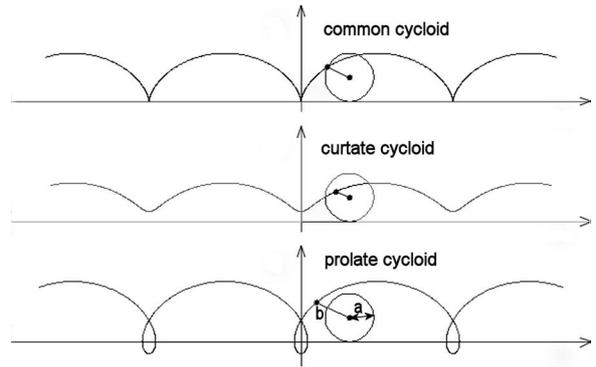


Fig. 3: Several forms of trochoids, also called common cycloid, curtate cycloid and prolate cycloid [19].

with  $\omega$  being the angular velocity of angle  $\phi$  rotating in time  $t$ :

$$\phi = \omega t. \tag{3}$$

For the  $x$  and  $y$  coordinates the parameter form of the cycloid is given by

$$x = a\phi - b \sin \phi, \tag{4}$$

$$y = a - b \cos \phi. \tag{5}$$

In the rest frame of the atom we have

$$v_e = \omega b \tag{6}$$

for the rotating electron. This equation determines the angular velocity  $\omega$ . The same  $\omega$  has to be used in formula (2). The roll radius  $a$  is determined then by the relative velocity  $v$ . If an observer tries to measure the diameter of a moving atom, he will see the reduced thickness of the cycloidal loop. For  $v = v_e$  we obtain  $a = b$ , the diameter goes to zero. For  $v > v_e$  there is only an unharmonic wave left and there is no measurable diameter of an atomic structure.

The diameter can be calculated quantitatively as follows. The  $x$  values for the diameter are defined by a vertical tangent of the cycloid, i.e.

$$\frac{dx}{d\phi} = 0, \tag{7}$$

which is according to Eq. (4):

$$a - b \cos \phi_0 = 0 \tag{8}$$

or

$$\phi_0 = \arccos \left( \frac{a}{b} \right). \tag{9}$$

Inserting  $\phi_0$  into (4) gives for the  $x$  values where the diameter is being measured

$$x_0 = a \arccos \left( \frac{a}{b} \right) - b \sqrt{1 - \frac{a^2}{b^2}}. \tag{10}$$

Since we have

$$x(\phi = 0) = 0 \tag{11}$$

the value  $x_0$  describes the radius of the atom measured from an observer frame with relative speed  $v$ . The well-known square root term is contained in this expression. To obtain this term exclusively we have to tentatively modify Eq. (4) by replacing  $a$  by another parameter  $a_1$ . Then we obtain from (10):

$$x_0 = a_1 \arccos\left(\frac{a}{b}\right) - b \sqrt{1 - \frac{a^2}{b^2}} \quad (12)$$

and in the limit  $a_1 \rightarrow 0$  the observed radius of the atom becomes

$$r = |x_0| = b \sqrt{1 - \frac{a^2}{b^2}}, \quad (13)$$

which with help of (2) and (6) can be rewritten to

$$r = b \sqrt{1 - \frac{v^2}{v_e^2}}, \quad (14)$$

which is the experimentally found expression for length contraction. So at least qualitatively we can explain length contraction from the geometric effect of relative circular motion.

#### 4 Special Relativity according to Einstein

We describe shortly the axiomatic foundation of special relativity as given by H. Ruder [1]. All physical conclusions follow from the Lorentz transformation. This can be derived from three postulates or axioms:

1. Homogeneity and isotropy of space;
2. Principle of relativity;
3. Constancy of light velocity.

The first axiom is foundational for all physics. The three-dimensional space free of masses has no places which are singled out from others and all directions are equivalent. From classical mechanics we know that these properties lead to the conservation laws of energy and angular momentum. Both statements are equivalent. Therefore axiom 1 is unsurmountable.

The relativity principle states that all inertial frames are equivalent for describing the laws of physics. A difference by measurement is not detectable. The prerequisite is that a global, absolute reference frame does not exist. This is at variance with general relativity as well as newer experiments explained in section 2. The relativity principle would be valid only if space were exactly homogeneous, i.e. free of matter. Then, according to general relativity and Mach's principle, the space would not exist at all. Therefore the relativity principle is a simplifying assumption which we will abandon in the following.

In the same way we do not claim absolute constancy of light velocity ( $c$ ) in all reference frames. From general relativity it follows that this velocity is not constant but dependent on the strength of the gravitational and other fields. One has

to negate this assumption even in special relativity as soon as optical refraction plays a role where the transmission speed of waves is  $v = c/n$  with  $n$  being the index of refraction.  $c$  can only be considered to be a value of light propagation in vacuo with absence of fields of every kind. Another way of circumventing the a priori assumption of a constant  $c$  is to measure the transformation law for the proper time of fast moving systems. In this way the well-known Myon experiment can be interpreted for example [1]. It comes out that the transformation law can be cast in a mathematical form containing a constant  $c$  which "may have something to do" with light propagation in vacuo. We conclude that only the first axiom has withstood a critical analysis.

#### 5 Modified Special Relativity according to this hypothesis

We will derive now the alternative theory resting upon the three fundamental assumptions:

1. Homogeneity and isotropy of space;
2. Existence of an absolute frame of reference;
3. Physical length contraction.

The first axiom has already been discussed. The second can be constituted by the fact that a more general theory, which does not presuppose inertial systems, allows a referencing system bound to the masses of the universe. Therefore it makes no sense to ignore this fact. If an absolute frame of reference is of physical relevance, it will have an effect. This is not so obvious from general relativity, because the gravitational field is no more effective outside the range of galaxies. It would be more plausible to have a principle of close-ranging or local interaction. In this class of principles belong the ether theories. Already Einstein talked of an "ether space" which was immaterial to his opinion. Sometimes new ether theories come up as for example by Schmelzer [2] where the ether has the property of mediating the principle "actio = reactio". An absolute frame of reference can be related to this ether. It is analogous to a medium for sound waves and the concept of non-homogeneity and the refraction index of wave propagation are applicable. This shows that an ether concept can be added to general relativity, if not already existing in it. An attempt to incorporate it into technical applications was made by Meyl [3].

The ether concept is not necessary when we base our considerations on a unified field theory like Einstein-Cartan-Evans theory [18]. Then space itself is a medium which shows optical properties and a local structure which is defined by the vacuum or background potential. The new interpretation of Michelson-Morley experiments is compatible with this concept.

As a third prerequisite we assume length contraction first introduced by Fitzgerald and Lorentz. As explained above this contraction is required to give consistent results of the

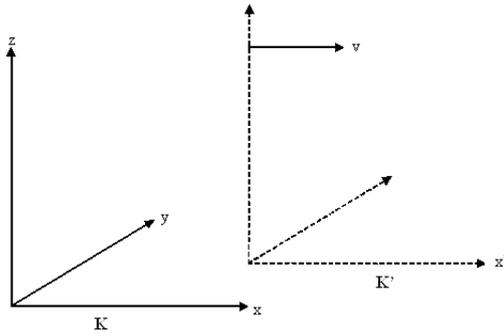


Fig. 4: Reference frames at rest ( $K$ ) and with relative motion ( $K'$ ).

interferometric experiments. If a body moves with velocity  $v$  relative to the background, all lengths are shortened by a factor of

$$\gamma = \sqrt{1 - \frac{v^2}{c^2}}. \quad (15)$$

This contraction is real and not an artifact of measurement. According to the considerations above this is an effect of relative motion. This factor also appears in electrodynamics where it describes the transformation law between electromagnetic fields. Matter exists on an electromagnetic basis. Consequently, this factor also appears in relativistic quantum mechanics. We will see in the next section that length contraction has an effect on time measurements so that local (“proper”) times of moving systems are impacted in the same way.

## 6 Derivation of the alternative theory

### 6.1 The transformation equations

In the following we will derive the transformation law between different reference frames. We will first give the transformation law of special relativity in the most general case as described in [1]. The result of the first axiom can be used directly because it is identical in Einstein’s and our theory. We define a coordinate system  $K$  at rest and a system  $K'$  moving with velocity  $v$  relative to  $K$ . The system  $K$  is the absolute rest frame as for example measured by experiment. Coordinate axes are chosen so that all axes between  $K$  and  $K'$  are in parallel, and motion is in  $x$  direction of system  $K$ . Then we can restrict consideration to one dimension. According to [1] the transformation law between  $K$  and  $K'$  then has the general form

$$x' = b(v)(x - vt) \quad (16)$$

$$x = b'(v')(x' + v't') \quad (17)$$

where  $b(v)$  and  $b'(v')$  are functions of the velocity. The second axiom has already been respected by assuming  $K$  to be at absolute rest. It should be noted that  $v$  is not an arbitrary relative velocity between any two frames but the velocity between the rest frame and another one.

Since the relativity principle is not valid it makes a difference if we transform from the resting to the moving system or backward. The functions  $b$  and  $b'$  therefore are different.  $b$  is defined by length contraction according to the third axiom. Since length contraction is real there is no symmetry between both systems. All length scales in moving systems are larger than in the rest system. The length  $l$  of a moving system measured from the rest system then is

$$l_0 = l \sqrt{1 - \frac{v^2}{c^2}}. \quad (18)$$

All scales are shrinking, i.e. for measuring the same length (the measured value read from a scale) in  $K'$  more scale units have to be used than in  $K$  if measurement is done when  $K'$  flies by in  $K$ . The length  $\Delta l$  (in units of  $K$  or  $K'$  respectively) transforms then as

$$\Delta l' = \frac{\Delta l}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (19)$$

and the function  $b$  from (16) is defined by

$$b = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}. \quad (20)$$

By backtransformation from  $K'$  to  $K$  we have to obtain the original length again, therefore

$$b' = b^{-1} = \sqrt{1 - \frac{v^2}{c^2}}. \quad (21)$$

If  $K'$  moves with  $v$ , observed from  $K$ , then  $K$  moves with  $-v$  observed from  $K'$ . This is the only place where the relativity principle remains valid. The sign of  $v$  however does not play a role in (20). The reversal of the sign of  $v$  has already been taken into account in Eqs. (16, 17). Therefore we can assume  $v = v'$  in the following.

As already mentioned, the length contraction also leads to a change in time scales as we can see from insertion of (16) into (17) (or vice versa) with regard of  $b$  and  $b'$ :

$$t' = bt = \frac{t}{\sqrt{1 - \frac{v^2}{c^2}}}. \quad (22)$$

In total we arrive at the complete non-symmetric set of transformation equations

$$x' = \frac{x - vt}{\sqrt{1 - \frac{v^2}{c^2}}}, \quad (23)$$

$$t' = \frac{t}{\sqrt{1 - \frac{v^2}{c^2}}}, \quad (24)$$

$$x = (x' + vt') \sqrt{1 - \frac{v^2}{c^2}}, \quad (25)$$

$$t = t' \sqrt{1 - \frac{v^2}{c^2}}. \quad (26)$$

So far we have considered only two inertial frames with one of them being at (absolute) rest. In case of several frames moving arbitrary to one another, none of them can be assumed to be the rest frame. Let us define two frames  $K'$  and  $K''$  whose coordinate origins move with speeds  $v_1$  and  $v_2$  relative to the rest frame  $K$ . then we have for the length contraction in both frames:

$$\Delta l' = \frac{\Delta l}{\sqrt{1 - \frac{v_1^2}{c^2}}}, \quad (27)$$

$$\Delta l'' = \frac{\Delta l}{\sqrt{1 - \frac{v_2^2}{c^2}}}. \quad (28)$$

Setting them in relation to each other directly gives

$$\frac{\Delta l'}{\Delta l''} = \sqrt{\frac{c^2 - v_2^2}{c^2 - v_1^2}} \quad (29)$$

or

$$\Delta l'' = \Delta l' \sqrt{\frac{c^2 - v_1^2}{c^2 - v_2^2}}. \quad (30)$$

Only in case  $v_1 \ll v_2$  this approximately results in the expression being know from special relativity:

$$\Delta l'' = \frac{\Delta l'}{\sqrt{1 - \frac{v_2^2}{c^2}}}, \quad (31)$$

where  $v_2$  is approximately the relative velocity between frames  $K'$  and  $K''$ . To derive the complete transformation law between  $K'$  and  $K''$  we first write the transformation of both frames from the rest frame:

$$x' = \frac{x - v_1 t}{\sqrt{1 - \frac{v_1^2}{c^2}}}, \quad (32)$$

$$t' = \frac{t}{\sqrt{1 - \frac{v_1^2}{c^2}}}, \quad (33)$$

$$x'' = \frac{x - v_2 t}{\sqrt{1 - \frac{v_2^2}{c^2}}}, \quad (34)$$

$$t'' = \frac{t}{\sqrt{1 - \frac{v_2^2}{c^2}}}. \quad (35)$$

Mutual insertion then gives the direct transformation

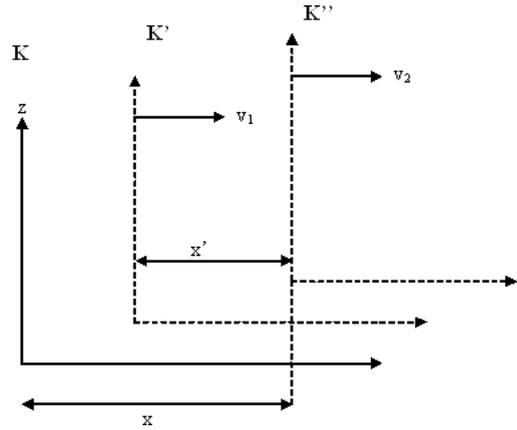


Fig. 5: Reference frames for addition theorem of velocities.

$K' \rightarrow K''$  as well as the reverse transformation  $K'' \rightarrow K'$ :

$$x'' = (x' - (v_2 - v_1)t') \sqrt{\frac{c^2 - v_2^2}{c^2 - v_1^2}}, \quad (36)$$

$$t'' = t' \sqrt{\frac{c^2 - v_2^2}{c^2 - v_1^2}}, \quad (37)$$

$$x' = (x'' + (v_2 - v_1)t'') \sqrt{\frac{c^2 - v_1^2}{c^2 - v_2^2}}, \quad (38)$$

$$t' = t'' \sqrt{\frac{c^2 - v_1^2}{c^2 - v_2^2}}. \quad (39)$$

Thus we have arrived at the general transformation laws between arbitrary frames of reference. For the back transformation the square root terms change to their inverse, and the sign of the  $vt$  term changes. These expressions cannot be reduced to a simple dependence on the speed difference  $v = v_2 - v_1$ . They depend on the absolute speeds of the inertial systems against the rest frame. Space and time coordinates transform with the same factor.

### 6.2 The addition theorem of velocities

We consider three coordinate systems  $K$ ,  $K'$  and  $K''$ . Frame  $K'$  is moving with velocity  $v_1$  relative to the rest frame  $K$  and  $K''$  with velocity  $v_2$  relative to  $K'$ . We will compute now with which velocity  $v_3$  then  $K''$  moves relative to  $K$  (Fig. 5). At time  $t = t' = t'' = 0$  all three coordinate origins shall coincide, so we have

$$x = v_3 t, \quad (40)$$

$$x' = v_2 t'. \quad (41)$$

The transformation equations (25–26) then with (41)

yield the connection between  $x(x', t')$  and  $t(t')$ :

$$x = (x' + v_1 t') \sqrt{1 - \frac{v_1^2}{c^2}} = (v_2 t' + v_1 t') \sqrt{1 - \frac{v_1^2}{c^2}}, \quad (42)$$

$$t = t' \sqrt{1 - \frac{v_1^2}{c^2}}. \quad (43)$$

By applying (40) the resulting velocity of  $K''$  is

$$v_3 = \frac{x}{t} = v_1 + v_2. \quad (44)$$

This is the addition theorem. The velocities add as vectors, in contrast to special relativity where we have the Einsteinian addition theorem (see Table 1). According to the latter, the sum of two velocities cannot exceed velocity of light. In this theory velocities add as vectors as in the Galilean transformation. The experimental consequences will be discussed in the subsequent section.

Now let's consider how velocities transform between frames directly. We assume that in  $K'$  and  $K''$  the same movement (for example of a mass) is measured locally by the velocities

$$v' = \frac{x'}{t'} \quad (45)$$

and

$$v'' = \frac{x''}{t''}. \quad (46)$$

By inserting (36, 37) into (46) we find

$$v'' = v' - (v_2 - v_1). \quad (47)$$

Velocities transform according to the Galilean transformation. In particular there is no limiting velocity.

## 7 Consequences

### 7.1 Comparison with Special Relativity

Both theories show a high degree of similarity, but there are some essential differences (see Table 1). In Einsteinian relativity the transformations are the same in both directions which is a consequence of the relativity principle. In the alternative theory the contraction factor reverses. This follows from the fact that this theory is based on an absolute frame of reference. This will be further discussed below.

There is a principal difference in the time transformations. In the alternative theory time is stretched by the same factor as length. In Einstein's relativity there is an additional term containing the space coordinate. So there is a coupling between space and time which ensures the basic axiom of constancy of  $c$ . In our theory space and time are decoupled, leading to a different metric. The coupling between space and time coordinates can be interpreted as follows. Consider two clocks in the rest frame, one at the coordinate origin and the other at location  $x = x_0, y = 0, z = 0$ . In Einstein's theory clocks

This Theory	Special Relativity
Coordinate Transformation	
$x' = \frac{x - vt}{\sqrt{1 - \frac{v^2}{c^2}}}$ $x = (x' + vt') \sqrt{1 - \frac{v^2}{c^2}}$ $y' = y$ $z' = z$ $t' = \frac{t}{\sqrt{1 - \frac{v^2}{c^2}}}$ $t = t' \sqrt{1 - \frac{v^2}{c^2}}$	$x' = \frac{x - vt}{\sqrt{1 - \frac{v^2}{c^2}}}$ $x = \frac{x' + vt'}{\sqrt{1 - \frac{v^2}{c^2}}}$ $y' = y$ $z' = z$ $t' = \frac{t - \frac{v}{c^2} x}{\sqrt{1 - \frac{v^2}{c^2}}}$ $t = \frac{t' + \frac{v}{c^2} x'}{\sqrt{1 - \frac{v^2}{c^2}}}$
Addition Theorem of Velocities	
$v_3 = v_1 + v_2$	$v_3 = \frac{v_1 + v_2}{1 + \frac{v_1 v_2}{c^2}}$

Table 1: Comparison of theories.

must be synchronized. When the first clock registers an event at  $x = 0, t = 0$ , this will be seen at  $x_0$  only after a delay which for light signals is  $t_0 = x_0/c$ . This delay of the measuring process is "built in" into special relativity and explains the appearance of the term  $(v/c^2)x'$  in the time transformation  $t(t')$  in Table 1.

In contrast to this, the alternative theory does not make any assumptions about measuring processes. Since there is no upper limit of relative velocities, it should be possible to construct an apparatus which measures a global time without significant delay. Such experiments have been discussed in section 1. Alternative methods of clock synchronization have been introduced by Tangherlini [7, 8, 9] who proposed a concept of a preferred frame similar to this work. He based his work (already done before 1958 [7]) on a partially instantaneous synchronization of clocks and arrived at transformation equations similar, but not identical, to ours. This corroborates that the measuring term  $x_0/c$  built into Einstein's theory is artificial. Tangherlini was not aware at that time of the anisotropy of  $c$  found experimentally in later years, for example by Cahill. Therefore he assumed full Lorentz invariance (i.e. isotropy) in each inertial frame. He defined the special form of time transformation so that it was consistent with his assumptions on clock synchronization. This is an essential difference to our work where the time transformation follows *by calculation* from the space transformation. Tangherlini obtained different values of  $c$  in each frame and a non-linear, direction dependent formula which relates these values to one another. In contrast, our calculation gives a vectorial addition

of all speeds including the signal transmission speed and relative frame speed. This is because we do not assume Lorentz invariance in each frame as Tangherlini did. Compared with the experiments of Cahill, our results are in accordance with them, but Tangherlini's are not.

Also in special relativity there is no real need for integrating signal transmission times into the transformation formulas. In addition, there are signal transmission speeds smaller than  $c$ , therefore it cannot be seen why experiments carried out with transmission velocity  $c$  should play a dominant role. If the space distance between clocks is known (and it can be measured of course), there is no problem to calculate the time of events at the other clock positions. This is like introducing time zones around the globe. We exactly know what time it is in other parts of the world without making any measurement. Occurrence of events at the same time can be defined by using the time of the rest frame.

While the Lorentz transformation represents a rotation in fourdimensional space, the transformation introduced by this theory has lower symmetry, it can be considered to be an affine mapping, i.e. a translation with stretching of scales. The transformation exhibits group properties as does the Lorentz transformation. This is shown in Appendix A in detail. We therefore conclude that the transformation introduced in this work can be used similarly to the Lorentz transformation as a basic property of higher developed theories, for example general relativity.

## 7.2 Comparison with known problems of Einsteinian theory

There are several interpretation problems in conventional special relativity. When comparing two frames being in motion to one another, the length rods of the other system appear shortened, seen from the system where the observer resides. This follows from the symmetry of the transformation law (Lorentz transformation). When the speed of one system is adopted to that of the other system, the difference in rod length disappears. At least Einstein has assumed that the scale change is a measuring artifact and not real.

Time dilation is regarded differently. In the well known twin paradoxon it is assumed that the integral taken over the coordinate time is identical to the real elapsed time, the scale change is considered to be a real effect as is done in general relativity. There is a contradiction in the interpretation. Contrary to this, the alternative theory assumes the scale changes always to be real. Since all length changes are related to the rest frame, there is no "symmetry" between measurements when one moving system measures quantities in another. For the twin paradoxon this means that the twin having higher absolute speed ages faster than the other one. Both twins can calculate the age of the other twin and come to the same result. All contradictions are removed.

The change of the time coordinate deserves further com-

ments. As is generally known the Lorentz transformation is a rotation in four dimensions, therefore the length of vectors is an invariant as can be expressed by

$$x^2 + y^2 + z^2 - c^2 t^2 = x'^2 + y'^2 + z'^2 - c^2 t'^2. \quad (48)$$

From this the differential invariance condition of the Minkowski metric follows:

$$dx^2 + dy^2 + dz^2 - c^2 dt^2 = dx'^2 + dy'^2 + dz'^2 - c^2 dt'^2. \quad (49)$$

To the knowledge of the author, experimental tests of special relativity, however, are not based on the invariance principle but on the coordinate transformations where the proper time of a moving system is computed by integrating the equation

$$d\tau = dt \sqrt{1 - \frac{v^2}{c^2}}. \quad (50)$$

Considering the time transformation for special relativity in Table 1, this equation should generally read

$$d\tau = \left( dt - \frac{v}{c^2} dx \right) \sqrt{1 - \frac{v^2}{c^2}}. \quad (51)$$

It is questionable if this formula ever has been tested experimentally. Experimenters always used setups where the simplified Eq. (50) was sufficient. These types of checks of special relativity have been made with very high precision. For testing the Lorentz transformation thoroughly, however, use of Eq. (51) would be required.

We conclude this section with a hint to relativistic mechanics which is also based on Eq. (50). Therefore the alternative theory gives the same results as special relativity, as far as the lab system can be identified within sufficient precision with the absolutely resting system. When experiments with light are performed, this is the case. Relativistic mechanics would look differently if experiments were performed in a fast moving lab relative to earth.

## 7.3 Comparison with newer experiments and final remarks

As a last point we bring to mind the experiments of Cahill et al. [10, 11] mentioned in sections 1 and 2. The authors stress that older experiments of Michelson-Morley type were two-way experiments, that means the distances in the interferometer were passed twice by light rays, in contrary directions. Thus a lot of information gets lost, and such experiments in vacuo are even meaningless as already mentioned. With use of modern electronics, one-way experiments have been carried out by Cahill et al. It could be shown that light velocity is indeed different in both directions compared to the motion of the earth relative to the space background. Even fluctuations in the background velocity were found. There is a full analogy to sound waves in media, with effects of speeds relative to the observer and of the refraction index. Similar experiments were carried out by de Witte [12]. Further independent

confirmations are required. There are certain measurements of Marinov [15, 16] which seem not to be consistent with Cahill's results, but it is not clear if the evaluation method of Marinov is compatible with that of Cahill and this work.

The concept of the refraction index can be used to produce superluminal processes by deploying special optical media with a refraction index  $n < 1$ . Obviously, the experiments of Nimtz [5, 6], who has transmitted audio data with superluminal speed, can be explained in this way. Since the input data (a symphony of Mozart) was recognized as such after the transmission, it is clear that useful signals can be transmitted with such a speed. The old argument that a "phase velocity"  $v > c$  cannot transport any information no longer holds. Thus our above statements are corroborated that a global time can be defined experimentally. Thornhill [14], and later Cahill [13], have further shown that Maxwell's equations, which are taken as an irrevocable proof that the Lorentz transform is incorporated in nature, can be formulated Galilei-invariant. Advanced theories like Einstein-Cartan-Evans theory [18] introduced a background potential and optical properties of space itself. Einstein's area is overcome. We conclude with a citation from Cahill [13]:

"The Special Relativity formalism asserts that only relative descriptions of phenomena between two or more observers have any meaning. In fact we now understand that all effects are dynamically and observationally relative to an ontologically real, that is, detectable dynamical 3-space. Ironically this situation has always been known as an "absolute effect". The most extraordinary outcome of recent discoveries is that a dynamical 3-space exists, and that from the beginning of Physics this has been missed — that a most fundamental aspect of reality has been completely overlooked".

## Appendix A: Proof of group properties

The transformation equations can be written in vector form with four-dimensional vectors and a transformation matrix:

$$\begin{pmatrix} x'' \\ y'' \\ z'' \\ t'' \end{pmatrix} = \begin{pmatrix} \alpha & 0 & 0 & -\alpha\beta \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & \alpha \end{pmatrix} \begin{pmatrix} x' \\ y' \\ z' \\ t' \end{pmatrix} \quad (\text{A-1})$$

with

$$\alpha := \sqrt{\frac{c^2 - v_1^2}{c^2 - v_2^2}}, \quad \beta := v_2 - v_1. \quad (\text{A-2})$$

This is — in contrast to the Lorentz transformation — not a rotation in 4-space but a linear transformation (stretching) with a translation. The determinant is  $\alpha^2$ , not unity as for the Lorentz transformation. Straight lines remain in parallel. The inverse transformation of (A-1) is

$$\begin{pmatrix} x' \\ y' \\ z' \\ t' \end{pmatrix} = \begin{pmatrix} \alpha^{-1} & 0 & 0 & \alpha^{-1}\beta \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & \alpha^{-1} \end{pmatrix} \begin{pmatrix} x'' \\ y'' \\ z'' \\ t'' \end{pmatrix} \quad (\text{A-3})$$

as can be verified by multiplication of both matrices. To compare this with the Lorentz transformation we rewrite above Eqs. (A-1, A-3) with Minkowski coordinates, i.e. with an imaginary time coordinate:

$$\begin{pmatrix} x'' \\ y'' \\ z'' \\ ict'' \end{pmatrix} = \mathbf{T} \begin{pmatrix} x' \\ y' \\ z' \\ ict' \end{pmatrix} \quad (\text{A-4})$$

with

$$\mathbf{T} = \begin{pmatrix} \alpha & 0 & 0 & i\alpha\beta \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & \alpha \end{pmatrix} \quad (\text{A-5})$$

and

$$\alpha := \sqrt{\frac{c^2 - v_1^2}{c^2 - v_2^2}}, \quad \beta := \frac{v_2 - v_1}{c}. \quad (\text{A-6})$$

Then we have in analogy to above:

$$\mathbf{T}^{-1} = \begin{pmatrix} \alpha^{-1} & 0 & 0 & -i\alpha^{-1}\beta \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & \alpha^{-1} \end{pmatrix} \quad (\text{A-7})$$

The set of transformations  $T(\alpha, \beta)$  is a commutative group. This is proven in the following by examining the group axioms.

### 1. Completeness

We define

$$\alpha_1 := \sqrt{\frac{c^2 - v_1^2}{c^2 - v_2^2}}, \quad \beta_1 := \frac{v_2 - v_1}{c}, \quad (\text{A-8})$$

$$\alpha_2 := \sqrt{\frac{c^2 - v_3^2}{c^2 - v_4^2}}, \quad \beta_2 := \frac{v_4 - v_3}{c}. \quad (\text{A-9})$$

Then we find for the concatenation of two transformations by matrix multiplication:

$$T(\alpha_1, \beta_1) T(\alpha_2, \beta_2) = T(\alpha_1\alpha_2, \beta_1 + \beta_2). \quad (\text{A-10})$$

### 2. Neutral element

The neutral element of the group is the unit matrix.

### 3. Inverse element

For each  $T(\alpha, \beta)$  there is an inverse transformation  $T^{-1} = T(\alpha^{-1}, -\beta)$ .

### 4. Associativity

The law of associativity for the matrix multiplication holds:

$$T(\alpha_1, \beta_1) [T(\alpha_2, \beta_2) T(\alpha_3, \beta_3)] = [T(\alpha_1, \beta_1) T(\alpha_2, \beta_2)] T(\alpha_3, \beta_3). \quad (\text{A-11})$$

### 5. Commutativity

From Eq. (A-10) directly follows

$$T(\alpha_1, \beta_1) T(\alpha_2, \beta_2) = T(\alpha_2, \beta_2) T(\alpha_1, \beta_1). \quad (\text{A-12})$$

So the group axioms have been proven.

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