

280(2a) : Dimensionality of the Continued Fraction

This is best seen by considering the continued fraction in the format:

$$\begin{aligned}\bar{\epsilon}(p) &= \frac{(\epsilon_0 - \epsilon_\infty) k_0(\omega) (p^2 + \gamma p + \kappa_1(\omega))}{p^3 + \gamma p^2 + (\kappa_0(\omega) + \kappa_1(\omega))p + \gamma \kappa_0(\omega)} \quad - (1) \\ &= (\epsilon_0 - \epsilon_\infty) \frac{k_0(\omega)}{p + \frac{\kappa_0(\omega)}{p + \frac{\kappa_1(\omega)}{p + \gamma}}}\end{aligned}$$

To recover the Debye theory:

$$k_0(\omega) = \frac{\kappa_0(\omega)}{\frac{p + \kappa_1(\omega)}{p + \gamma}} \quad - (2)$$

so:
$$\bar{\epsilon}(p) = (\epsilon_0 - \epsilon_\infty) \frac{k_0(\omega)}{p + k_0(\omega)} \quad - (3)$$

where
$$k_0(\omega) = \frac{1}{\tau} \quad - (4)$$

The dimensionality of $k_0(\omega)$ is s^{-1} , the dimensionality of $\kappa_0(\omega)$ and $\kappa_1(\omega)$ is s^{-2} , and that of $\bar{\epsilon}(p)$ is dimensionless