

292(3): Some Examples of Spectra for the Calculation of Evans / Mori Shifts.

In general the shifts are given by:

$$\frac{\omega_1^4}{\left(\exp\left(\frac{\hbar\omega_1}{kT}\right) - 1\right)} = \frac{\omega^4}{\left(\exp\left(\frac{\hbar\omega}{kT}\right) - 1\right)} \exp(-d\tau) \quad - (1)$$

If
and

$$\hbar\omega_1 \ll kT \quad - (2)$$

$$\hbar\omega \ll kT \quad - (3)$$

then:

$$\boxed{\left(\frac{\omega_1}{\omega}\right)^3 = \exp(-d\tau)} \quad - (4)$$

It is seen that the ratio of refracted frequency ω_1 to incident frequency ω depends directly on the power absorption coefficient d . Some types of spectra are given below from Omic Opera II.

Pure Rotational Envelope.

$$d \propto (2J+1) \exp\left(-\frac{E}{kT}\right) \quad - (5)$$

2) where:

$$E = hcB J(J+1) \quad - (6)$$

where B is the rotational constant in wavenumbers and J the rotational quantum number

Dipole Induced Dipole Absorption

$$d(\omega) \propto \left(1 - \exp\left(-\frac{2B(J+1)hc}{kT}\right) \right) 2B(J+1) \exp\left(-\frac{BJ(J+1)hc}{kT}\right) \\ \times \left(4d_0^2(J+1) + \frac{8}{3}\delta^2 \frac{(J+1)^2(J+2)}{2J+3} \right)$$

where $d_0 = \frac{1}{3}(d_{||} + 2d_{\perp})$, $\delta = (d_{||} - d_{\perp})$. - (7)

Hexadecapole Induced Dipole Absorption

$$d(\omega) \propto 4B(2J+5) \left(1 - \exp\left(-\frac{4B(2J+5)hc}{kT}\right) \right) \exp\left(-\frac{BJ(J+1)hc}{kT}\right) \\ \left[\frac{175(J+1)(J+2)(J+3)(J+4)d_0^2}{2(2J+3)(2J+5)(2J+7)} - (8) \right. \\ \left. + \frac{875}{12}\delta^2 \left(\frac{(J+1)(J+2)}{(2J+3)} \right)^2 \frac{(J+3)(J+4)}{(2J+5)(2J+7)} \right]$$

Here:

$$\omega = 2\pi \bar{\nu} c = 2\pi f \quad - (9)$$

and B is expressed in units of wavenumber $\bar{\nu}$ in

cm^{-1} . So:

$$f = \bar{\nu} c \quad - (10)$$

The hexadecapole moment of oxygen was measured in 0011.

The easiest type of spectrum to evaluate is the pure rotational spectrum (5), where:

$$J = 0, 1, 2, \dots$$

and

$$\Delta J = 1 \quad - (11)$$

The spectrum is a series of lines with an envelope given by the Boltzmann factor $\exp(-E/(kT))$ and its degeneracy $(2J+1)$.

For each absorption line there is an Evans/Moris shift.

Therefore an incident beam of incident frequency ω enters a sample cell filled with gas. The beam is refracted and absorbed, and its frequency is changed by an Evans Moris shift according to eq. (1), approximated by eq. (2). For dipole induced dipole absorption the selection rule is again $\Delta J = 1$, but for hexadecapole dipole absorption it is $\Delta J = 4$ (0011).
